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This issue marks the third year of existence of the *African Journal of Computing & ICT*. It is a combined issue containing both the first and second edition of Volume 3.

This volume contains four (4) papers which are on information retrieval system, foundations of computer science/discrete structures and numerical computation.

In his paper entitled, “Comparative Study of Some Popular Web Search Engines”, Dr. Olalekan Akinola evaluated the effectiveness of 5 popular search engines (namely, Google, MSN, Alta Vista, 37.com and Yahoo) by using a list of 15 computer science-related keywords/queries. It was established, among others, that Google has the highest document retrieval efficiency (in terms of the total number of documents retrieved), followed by Yahoo, Alta Vista, MSN and 37.com. This result confirms the earlier results obtained by Griesbaum (2004), and Hananzita and Kiran (2006). The paper also confirmed the result of Hong and David (2007) to the effect that Google always takes a very small time to retrieve a document.

Prof. ‘Dele Oluwade’s paper on ‘The Galois Group of the Chebyshev Polynomials of the First Kind of Prime Degree’ is a study on the Galois group theoretical structure of the Chebyshev Polynomials of the first kind of prime degree. The Galois group is a discrete structure which arises from the Galois theory of equations propounded by the famous French scientist Evariste Galois (1811-1832). This group provides a connection between the algebraic theory of fields and group theory. By first finding the splitting field of the polynomials over the set of rational numbers, the author showed that the Galois group of the polynomials is isomorphic to the cyclic group of order two.

The paper by Dr. O.A. Taiwo and A.K. Bello dwelt on the numerical solution of boundary value problems via Patched Segmented Collocation Method in which the whole intervals of consideration have been partitioned into various subintervals. In the paper, the solutions are first sought in the various subintervals and thereafter matched together using Chebyshev Polynomials as the basis function. By using numerical examples, the authors established the efficiency and accuracy of the method, demonstrating that the results obtained are better than when problems are solved within the whole intervals.
In ‘A Note on the Algebra of Qualitative Equivalence of Ordinary Differential Equations’, Prof. Dele Oluwade presented an exposition on the notion of qualitative equivalence of ordinary differential equations. This is a concept which assists in describing the behavior of an equation without necessarily drawing the solution curves of the equation. Qualitative equivalence of a set of differential equations naturally leads to the generation of the qualitative classes of the set, which is a discrete structure. In the paper, the author generated the qualitative classes of a simple example of a set of first order autonomous ordinary differential equations. Practical areas of application of the concept of qualitative equivalence include computer networking, fractals and coding theory.
COMPARATIVE STUDY OF SOME POPULAR WEB SEARCH ENGINES

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ABSTRACT
Web search engines are veritable tools for information mining. These search engines differ in effectiveness at retrieving relevant documents from the web. A big question is “which search engine(s) is/are best to use in specific instances?” This work evaluates effectiveness of five search engines on fifteen Computer Science queries. Measures obtained from this study include search output quantity, search time, relevant documents retrieved, search precision and the quantity of African contents in the search. Briefly the study shows that (1) the fact that a Web search engine is very popular and able to retrieve large number of documents does not mean that it has high precision for retrieving relevant documents for its users and (2) Africa has contributed little or nothing to the global Web contents in the field of Computer Science. However, this work needs to be extended to other academic areas in order to generalize these results.

Keywords: Information Retrieval, Effectiveness, Web, Search Engine
I. INTRODUCTION

The World Wide Web (Web) is one of the largest publicly available databases of documents on the Internet [9]. It is a good testing ground for most information retrieval techniques.

The growth of the Web is an unprecedented phenomenon. Four years after its birth in 1990, a million or more copies of the first well-known Web browser, Mosaic, were in use [1]. This growth was a result of the exponential increase of Web servers and the value and number of web pages made accessible by these servers. In 1999 the number of Web servers was estimated at about 3 million and the number of web pages at about 800 million [18], and three years later, in June 2002, the search engine AlltheWeb, announced that its index contained information of about 2.1 billion web pages [9].

There are millions of Web users and about 85% of them use search engines to locate information on the Web [17]. It is discovered that search engine use is the second most popular Internet activity next to e-mail [15]. Due to high demand there are hundreds of general purpose and thousands of specialized search engines on the Internet today.

A Web search engine is an information retrieval system [20], which is used to locate the Web pages relevant to user queries. Search engines for the general web do not really search the Web directly. Each one searches a database of the full text of Web Pages selected from the billions of Web pages out there residing on servers. When the web is searched using a search engine such as Google or Alta Vista, a somewhat stale copy of the real web page is searched. When we click on links provided in a search engine’s search results, we retrieve the current version of the Web page [6].

Search engine databases are selected and built by computer robot programs called Spiders [22]. Although it is said that they “crawl” the web in their hunt for pages to include, in truth they stay in one place. They find the pages for potential inclusion by following the links in the pages they already have in their database (that is, already “know about”). They cannot think or type a Universal Resource Locator (URL) or use judgment to “decide” to go and look something up and see what is on the web about it.

If a Web page is never linked to any other page, search engine spiders cannot find it. The only way a brand new page, one that no other page has ever linked to, can get into search engine companies is by requesting that the new page be included. All search engine companies offer ways to do this. After spiders find pages, they pass them on to another computer program for “indexing”. This program identifies the text, links and other content in the page and stores it in the search engine database’s files so that the database can be searched by keyword and whatever more advanced approaches are offered, and the page will be found if the search query matches its content.
The motivation we have for this study is based on the fact that identifying the most effective Web search engines (among the popular ones we use everyday) satisfying the current information needs is important both at personal and business levels. The results of this research can be used for (a) finding more relevant documents with less effort; (b) finding out which of these popular search engines is most appropriate and effective for searching documents for academic and research purposes and (c) motivating search engine providers for higher standards.

In this paper, our case study was based on five search engines, which are frequently used by Internet users when sourcing for information on the Internet [4]. These are Google (www.google.com), Microsoft Network (MSN, www.msn.com), Alta vista (www.altavista.com), 37 (www.37.com) and Yahoo (www.yahoo.com) search engines. A list of fifteen computer science – related keywords was searched with these search engines and the following information obtained from them: Quantity of search output (that is, effectiveness), time used for the search, the advert content, relevant results and the number of African contents.

Results from the study have great implications for both students and academics using Internet for finding information for their academic endeavours.

This paper is organized as follows. In section 2 we give an overview of some related works. We then explain the methodology and or experimental set up in terms of queries and search engines involved in Section 3. Detailed experimental results and discussion on them are presented in Section 4. Conclusion and recommendations are finally presented in Section 5.

II. LITERATURE REVIEW

The explosive growth of the Internet has rendered the World Wide Web as the primary tool for information retrieval today [12]. Adeyemo and Osunade [2] assert that in Africa research institutions, universities and media houses are the major users of the Internet. A survey of 1000 academics in 10 of the universities in Nigeria shows that the web, one of the internet resources, is used by 92.5% of the academics surveyed [3]. According to Choo, et al. [23], people use the Web as information resource to support their daily work activities and engage in a range of complementary modes of information seeking.

For information retrieval purposes on the Web, most people use search engines like Google, Yahoo and MSN. Sullivan [24] and Griesbaum [11] assert that Google is the dominant and most successful search engine among its contemporaries. For assessing the performance of these search engines, there are various measures such as database coverage, query response time, user effort and retrieval effectiveness, that can be used [9]. The dynamic nature of the Web also brings some more performance measure concerns regarding index freshness and availability of the Web pages as time passes [5]. The most common effectiveness measures are
**precision** (ratio of retrieved relevant documents to the total number of retrieved documents) and **recall** (ratio of retrieved relevant documents to the total number of relevant documents in the database) [9].

Measuring the search engine effectiveness is expensive due to the human labour involved in judging relevancy. This has been reported in several studies [9, 13]. Evaluation of search engines may need to be done often due to changing needs of users or the dynamic nature of search engines (for example, their changing Web coverage and ranking technology) and therefore it needs to be efficient [9].

Per Thousand Precision approach was formulated and used for computing the precision of the search engines used in this study. Since we based our human judgment on the first 1000 top documents retrieved for the relevant documents retrieved by the search engines, we therefore adopted this approach, although the first top 20 documents are commonly used [16].

There are two types of search engine evaluation approaches in the literature: testimonial and shootout [9]. Testimonials are casual studies and state the general impression obtained after executing a few queries. Shootouts are rigorous studies and follow the information retrieval measures for evaluation purposes. Our approach in this study is of the type shootout. The Jansen and Pooch [15] study provides an extensive review and analysis of current Web searching results. It provides a rich reference list and proposes a framework for future research on Web searching.

In addition, the Gordon and Pathak [10] study, which measures the performance of eight search engines using 33 information needs also recommends seven features to maximize the accuracy and informative content of such studies (see Table 1 below). Hawkins et al., [13] also proposes some more features in addition to the seven items specified in Gordon and Pathak [10] (also in Table 2.1)
Table 2.1: Desirable features of Web search evaluation according to Gordon and Pathak [10]: features 1 to 7 and Hawking et al.,[13]: features 8-11.

1. The searches should be motivated by genuine information needs of Web users.
2. If a search intermediary is employed, the primary searcher’s information need should be captured as fully as and with as much context possible and transmitted to the intermediary.
3. A sufficiently large number of searches must be conducted to obtain meaningful evaluations of search engines’ effectiveness.
4. Most major search engines should be considered.
5. The most effective combination of specific features of each search engine should be exploited (i.e. the queries submitted to the engines may be different).
6. The user who needs the information must make relevance judgments.
7. Experiments should (a) prevent bias towards search engines (e.g. by blinding or randomizing search outputs), (b) use accepted information retrieval measures, (c) employ statistical tests to measure performance differences of search engines.
8. The search topics should represent the range of information needs over which it is desired to draw conclusions.
9. Result judging should be appropriate to the type of query submitted (e.g. some queries may need a one-line answer).
10. Document presentation should be like that of a Web browser (images should be viewable, if necessary, it should be possible to follow links).
11. Dead links should count as useless answers.

Source: (Fazli, et al, [9]).
In this study, we satisfy most of the features given in Table 1 above. Features 2 and 5 are exceptionally disregarded in this study. Feature 2 does not really apply to us and contrary to the suggestions of the authors, in such studies we believe that genuine user queries should be used. By this way, the true everyday behaviour of the search engines will be measured [9]. Feature 5 needs expert searchers claiming that the best query formulation should be used for a specific search engine. Since most Web searchers in real life are casual users, we therefore disagree with this point. In the Web environment, there is no standardized test collection with complete relevance judgments [13]. Therefore we could only satisfy 6 to a little extent in this study. Being the dynamic and huge environment that it is, makes it almost impossible to determine such a collection and to obtain human relevance judgments, since it would be too cumbersome for people to judge so many Web pages.

Literature shows that several studies have been carried out by researchers in line with all these features with some modifications and / or enhancements [7, 19, 21]. For instance, Griesbaum [11] compares the performances of three German search engines – Altavista, Google and Lycos – in terms of relevance and precision using 50 queries. Results from his study shows that Google reached the highest values, followed by Lycos and then AltaVista. Hananzita and Kiran [12] also compare the performances of four Malaysian web search engines using Google as the benchmark search engine. Their results also show that Google outperforms the four engines considered.

III. METHODOLOGY / EXPERIMENTAL SET UP

III.1 User Queries

Measuring retrieval effectiveness requires user queries. For the construction of the queries used in this study, fifteen Computer Science – related information needs (queries) were described in terms of keywords that were to be used for the study. These keywords covered a broad range of topics in Computer Science profession. The study used AND and OR Boolean operators when the keywords were given to the search engines to search. The following keywords were used for this study:

1. Algorithms (ALG)
2. Data Structures (DS)
3. J2Me
4. Operating Systems (OS)
5. Database Management Systems (DBMS)
6. Hacking (HK)
7. Microprocessors (MP)
8. Recursion (RC)
9. Software (SW)
10. Compilers (CP)
11. Optical Character Recognition (OCR)
12. Networking (NW)
13. World Wide Web (WWW)
14. Multimedia (MM)
15. Artificial Intelligence (AI)

III.2 Search Engines

Five popular search engines among students and academic researchers [4] were selected in conducting our experiment. They are as mentioned in the
penultimate paragraph of Section 1 of this paper.

**III.3 Performance Evaluation Measures**

Based on the keywords used in the experiment, we aim at assessing the individual search engines based on:

i. **Quantity** of documents retrieved by the engines;

ii. **Time taken** for each keyword search to be completed by the engines (Response time): while three of the search engines (Yahoo, MSN and Google) reported their time of search as part of their results we measured this manually by a digital timer for those that do not have the timing facility (Alta vista and 37.com);

iii. **Per Thousand Precision** of documents retrieved: we observed and recorded the number of results that gave us relevant information about the keywords used, divide this by the total number of documents retrieved and finally multiplied by 1000 (reason aforementioned);

iv. **Advert Content**: for each search engine, we observe the amount of commercial-oriented documents produced at each keyword searched; and

v. **African content**: we enlisted this criterion to determine how much has the African continent as a whole been able to establish herself in the world of computer science today. We determine this by scrutinizing the information given by the links to see if we can find any African related author’s name and address.

**III.4 The Search Process**

In this step, we used the queries formulated and submitted them to the chosen search engines. For each keyword given to the search engines, we diligently took all the performance evaluation measures as indicated in subsection 3.3 above. All the experiments were done on a Pentium 4 MMX, 40MB, 2.0MHz computer located in the Ayo Rosiji Research Laboratory, at the Kola Daisi Building, in the Department of Computer Science, University of Ibadan, Nigeria on 11 – 16 October, 2008. For the measures of Advert content and African content, we based our human judgment on the top 1000 documents retrieved by the search engines. The only exception is the 37.com search engine, of which total documents retrieved are always less than 50.

**IV. EXPERIMENTAL RESULTS**

**IV.1 The Search Engines’ Performances**

Table 4.1 gives the quantity of documents (Q), retrieved and time taken (T) in seconds for each query given to the search engines. The keywords or queries are abbreviated in the table simply for space purposes but they were used directly as normal texts for the search study.
Table 4.1: Quantity of Documents retrieved (Q) and Time in Seconds (T)

<table>
<thead>
<tr>
<th>S/N</th>
<th>Query (Key Words)</th>
<th>Google Q</th>
<th>Google T</th>
<th>MSN Q</th>
<th>MSN T</th>
<th>Yahoo Q</th>
<th>Yahoo T</th>
<th>Alta Vista Q</th>
<th>Alta Vista T</th>
<th>37.com Q</th>
<th>37.com T</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>ALG</td>
<td>9240000</td>
<td>0.16</td>
<td>1583408</td>
<td>0.19</td>
<td>110000</td>
<td>0.15</td>
<td>224813</td>
<td>0.50</td>
<td>34</td>
<td>0.54</td>
</tr>
<tr>
<td>2.</td>
<td>DS</td>
<td>7270000</td>
<td>0.19</td>
<td>1739483</td>
<td>0.23</td>
<td>435115</td>
<td>0.10</td>
<td>7516787</td>
<td>0.59</td>
<td>11</td>
<td>0.64</td>
</tr>
<tr>
<td>3.</td>
<td>J2ME</td>
<td>726000</td>
<td>0.16</td>
<td>207605</td>
<td>0.19</td>
<td>67500</td>
<td>0.40</td>
<td>125157</td>
<td>0.50</td>
<td>33</td>
<td>0.54</td>
</tr>
<tr>
<td>4.</td>
<td>OS</td>
<td>11600001</td>
<td>0.18</td>
<td>6255462</td>
<td>0.22</td>
<td>1000000</td>
<td>0.75</td>
<td>3674348</td>
<td>0.56</td>
<td>29</td>
<td>0.61</td>
</tr>
<tr>
<td>5.</td>
<td>DBMS</td>
<td>8820020</td>
<td>0.17</td>
<td>171494</td>
<td>0.20</td>
<td>105423</td>
<td>0.20</td>
<td>177320</td>
<td>0.53</td>
<td>34</td>
<td>0.57</td>
</tr>
<tr>
<td>6.</td>
<td>HK</td>
<td>5370000</td>
<td>0.15</td>
<td>1305195</td>
<td>0.18</td>
<td>795112</td>
<td>0.60</td>
<td>1992876</td>
<td>0.47</td>
<td>31</td>
<td>0.51</td>
</tr>
<tr>
<td>7.</td>
<td>MP</td>
<td>1180120</td>
<td>0.18</td>
<td>243040</td>
<td>0.22</td>
<td>124133</td>
<td>0.15</td>
<td>266029</td>
<td>0.56</td>
<td>33</td>
<td>0.61</td>
</tr>
<tr>
<td>8.</td>
<td>RC</td>
<td>753000</td>
<td>0.16</td>
<td>113116</td>
<td>0.19</td>
<td>1000000</td>
<td>0.65</td>
<td>161083</td>
<td>0.50</td>
<td>27</td>
<td>0.54</td>
</tr>
<tr>
<td>9.</td>
<td>SW</td>
<td>23500000</td>
<td>0.16</td>
<td>8123</td>
<td>0.19</td>
<td>1315000</td>
<td>0.15</td>
<td>48117366</td>
<td>0.50</td>
<td>38</td>
<td>0.54</td>
</tr>
<tr>
<td>10.</td>
<td>CP</td>
<td>5910000</td>
<td>0.15</td>
<td>364205</td>
<td>0.18</td>
<td>652000</td>
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<td>525593</td>
<td>0.47</td>
<td>34</td>
<td>0.51</td>
</tr>
<tr>
<td>11.</td>
<td>OCR</td>
<td>2770000</td>
<td>0.19</td>
<td>74879</td>
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<td>50000</td>
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<td>58903</td>
<td>0.59</td>
<td>30</td>
<td>0.64</td>
</tr>
<tr>
<td>12.</td>
<td>NW</td>
<td>22500000</td>
<td>0.14</td>
<td>3390131</td>
<td>0.17</td>
<td>1100000</td>
<td>0.60</td>
<td>6606411</td>
<td>0.44</td>
<td>7</td>
<td>0.47</td>
</tr>
<tr>
<td>13.</td>
<td>WWW</td>
<td>8230000</td>
<td>0.14</td>
<td>34783984</td>
<td>0.17</td>
<td>85000000</td>
<td>0.15</td>
<td>71309208</td>
<td>0.44</td>
<td>32</td>
<td>0.47</td>
</tr>
<tr>
<td>14.</td>
<td>MM</td>
<td>35900000</td>
<td>0.17</td>
<td>13588351</td>
<td>0.20</td>
<td>73000000</td>
<td>0.30</td>
<td>46</td>
<td>0.53</td>
<td>15</td>
<td>0.57</td>
</tr>
<tr>
<td>15.</td>
<td>AI</td>
<td>34000000</td>
<td>0.16</td>
<td>776817</td>
<td>0.19</td>
<td>3300000</td>
<td>0.40</td>
<td>625816</td>
<td>0.50</td>
<td>31</td>
<td>0.54</td>
</tr>
<tr>
<td>MEAN</td>
<td></td>
<td>23745076</td>
<td>0.16</td>
<td>4307019</td>
<td>0.20</td>
<td>10945619</td>
<td>0.41</td>
<td>9560338</td>
<td>0.51</td>
<td>28</td>
<td>0.55</td>
</tr>
</tbody>
</table>
Fig. 4.1: Mean Quantity (Q) of Documents Retrieved by the Search Engines
The data presented in Table 4.1 and Figs. 4.1 and 4.2 above reveals that Google search engine has the highest document retrieval efficiency in terms of total number of documents retrieved (mean = 23,745,076) for all the queries (key words) given. This trend is followed by Yahoo (mean = 10,945,619), Alta vista (mean = 9,560,338), MSN (mean = 4,307,019) and 37.com (mean = 28) in that order. This result is in line with the ones obtained by Griesbaum [11] and Hananzita and Kiran [12] where Google was reported to have the highest document retrieval from the Web. Time, on the other hand followed a reverse trend. The search engine with the minimum document retrieval efficiency (37.com) has the highest time taken (mean = 0.55s) for retrieving the few number of documents. This is followed by Alta vista (mean = 0.51s) and Yahoo (mean = 0.41s), which have more or less the same mean number of documents retrieval efficiency. Google and MSN have comparable mean time values of 0.16s and 0.20s respectively. Hong and David [14] also
demonstrate that Google always take a very small time for document retrieval on the Web.

IV.2 Relevant Documents Retrieved (Precision) and Advert Content

Table 4.3 gives the quantity of relevant results from the searches, which we eventually computed as Per Thousand Precision (PTP) and the advert contents in the top 1000 documents retrieved by the search engines. The only exception is the 37.com, which does not seem to have good efficiency for all the queries used in the study. We only considered the top 1000 documents retrieved by the search engines in order to determine these measures since it is time and effort costly to go through all the documents retrieved by these search engines one by one, less for the 37.com. Even the top 1000 documents chosen for this study was very time consuming and strenuous as we have to click on each of their links to see what contents they have.

In the table, the advert content (AC) gives the total number of documents that are advertising in nature possibly for selling books or software or asking the web user to subscribe to journals or publishers in charge of the documents. Per Thousand Precision (PTP) is calculated thus:

\[
PTP = \frac{\text{Total number of retrieved relevant documents} \times 1000}{\text{Total number of retrieved documents}}
\]

There are some overlaps in the advert and relevant documents retrieved in that some documents contain advertisement and at the same time having some useful introduction and/or information about the subject matter of the query. Some of the documents that we cannot classify into any of these two categories were simply disregarded for these measures in the study.
Table 4.3: Advert Content (AC), Relevant Documents Retrieved (R) and Per Thousand Precision (PTP)

<table>
<thead>
<tr>
<th>S/ N</th>
<th>Query (Key Words)</th>
<th>GOOGLE</th>
<th>MSN</th>
<th>YAHOO</th>
<th>ALTA VISTA</th>
<th>37.COM</th>
</tr>
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<tbody>
<tr>
<td></td>
<td>AC</td>
<td>R</td>
<td>PTP</td>
<td>AC</td>
<td>R</td>
<td>PTP</td>
</tr>
<tr>
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<td>ALG</td>
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<td>563</td>
<td>0.061</td>
<td>250</td>
<td>267</td>
</tr>
<tr>
<td>2</td>
<td>DS</td>
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Note: PTP values are rounded to three decimal places.
Fig. 4.3: Chart of Advert Content (AC), Relevant Documents (R), and Precision (PTP) versus the Search Engines
Table 4.3 and Fig. 4.3 above reveals that Yahoo search engine has the highest Mean Advert Content (AC, mean = 538) followed by Alta vista (mean = 383), Google (mean = 333), MSN (mean = 331) and 37.com (mean = 9) in that order.

In the case of Mean Relevant Documents Retrieved (R), Google has the highest (mean = 664) followed by Alta vista (mean = 564), MSN (mean = 345), Yahoo (mean = 169), and 37.com (mean = 17), in that order. This result is in consonance with the work of Griesbaum [11] in which Google had the highest relevance followed by Lycos and AltaVista in that order.

In the case of Mean Per Thousand Precision, which is one of the universal methods of determining the effectiveness of web search engines, 37.com happens to have the highest (mean = 619.41), followed by Alta vista (mean = 53.67), MSN (mean = 2.22), Yahoo (mean = 0.96) and Google (mean = 0.40) in that order. Griesbaum [11] shows that differences of precision between Google, lycos and Alta Vista are very low. Therefore, the result obtained for Google having highest relevance initially and now with the lowest precision is fairly justified. Hananzita [12] asserts that recall by itself is not a good measure of the quality of a search engine. The precision gives more information about a search engine’s effectiveness at retrieving relevant documents from the Web.

IV.3 African Content

The African content (AF) is the total number of documents we adjudged to be African in nature, that is, documents we found that the author’s name or the author’s address comes from Africa. Only two of the keywords searched were able to be African in nature. These are Hacking and Multimedia. Yahoo search engine was able to retrieve 2 documents for the Hacking keyword, which we really found to be African in nature. One of the documents was a Nigerian Newspaper report on electronic hacking problem in Nigeria. The other document seems to come from Ghana from the author’s address seen. With Multimedia keyword, MSN retrieved one document, which actually comes from South Africa.

V. DISCUSSION OF RESULTS

Web search engines are meant for information retrieval for academic and research purposes among others. These search engines are numerous and new ones are springing up everyday on the Internet. The main question is “which of the existing search engines is / are very effective for information retrieval on the web for a specific purpose?” Effective measures are done via the total documents retrieved, time taken for the retrieval, effort expended and most importantly the precision and recall of the documents retrieved.

Google seems to have the best documents retrieval performance in terms of mean number of documents retrieved and relevance with little time of search. However, it has the least effectiveness in terms of precision. The results show that the fact that a search engine brings out large quantity of documents when used for Web search does not mean that it is highly effective. What this suggests are that (1) possibly some of the documents retrieved may have ‘dead links’ since stale copies of the universal resource locator (URL) addresses of the documents are also
indexed and stored in the search engine’s database. It is when the links to them are clicked that the search engine will go and look for the current version of the documents, which might have been moved or no more valid; and (2) possibly most of the documents retrieved are advertising in nature. They may not contain the information needed by the searcher at a particular period of time. More so, Google is a very popular search engine and since many people, institutions and organizations are associating themselves with it, it therefore means that the search engine would be a good avenue for advertising software products and books on the Web.

Yahoo being another popular search engine follows the same trend as Google. It also has good document retrieval capacity and response time. However, its average precision is very low (0.96). Its advert content is the highest in the study. This means that if a searcher is looking for journal subscription or buying books and products online, Yahoo and Google will be the better search engines to use.

MSN does not seem to have good document retrieval efficiency but its relevant documents retrieved as well as precision are encouraging. Alta Vista has good document retrieval efficiency as well as relevant documents retrieved and precision. This means that it is both useful for advertisement and relevant information retrieval purposes.

37.com search engine performs worst in terms of quantities of documents retrieved and response time for the keywords used in this study. However, it has the best relevance and precision. Although this search engine has the least document retrieval efficiency, this may be attributed to the fact that the main focus of the organization in charge of the search engine may not be in Computer Science profession or that its database might not have been fortified with documents in this domain as at the time this study was done. Actually, we are able to find out practically that most of the few documents retrieved by this search engine is always relevant to our information need. As such, we conclude that 37.com would be a very good search engine for researchers in the nearest future, although we need to verify this fact with information needs of some other professions.

By and large, our results in this study are in line with most of the previous findings in the literatures [9, 10, 13]. In a survey conducted by Enid [8] Google, Yahoo and MSN continue to be the most searched engines with Google taking 48.3%, Yahoo, 27.5% and MSN 10.9% United States (US) search market share in 2007. The main point is that results from this study has demonstrated that the fact that a Web search engine is very popular and able to retrieve large number of documents does not mean that it has high precision for retrieving relevant documents for its users.

A very interesting result in this study is the fact that African contents on the web are nothing to write home about. This means that Africa has not contributed meaningfully to the global web content in the field of Computer Science.

VI. CONCLUSION AND RECOMMENDATIONS

In this study we present an experiment to evaluate the performance of some popular web search engines. We measure the performance of the search engines after examining various numbers of top pages
returned by the search engines and then determine the mean document quantities retrieved, time taken (response time) for the retrieval, documents’ relevance, advert content, African content and precision for each search engines. In the experiment we use 15 Computer Science – related queries and look at their performances on five different search engines based on human relevance judgments of users.

Our experiments show that there are differences in the performance of these search engines in the research domain (Computer Science). Summarily, the study shows that:

(i) Google, MSN and Yahoo search engines have high document quantity retrieval capacity with low response time but their effectiveness (precision) in retrieving relevant documents is very low. They are good avenues for advertisement on the Web;
(ii) Alta vista search engine is very good for both relevance and advertisement;
(iii) 37.com search engine, although may bring out low document quantity retrieval but most of these documents will be relevant to the information needs of the searcher; and
(iv) Africa is yet to contribute meaningfully to the global web contents especially in the field of Computer Science.

Knowing the most effective Web search engines satisfying the current information need is important both at personal and business enterprise levels. However, the definition of “the best” changes due to both the changing information needs of users and the changing quality and nature of search engines. Accordingly, for different information needs from different professionals, the most effective search engine may be different. Hence, search engine performance needs to be tested and should be done quite often. Based on this recommendation, we therefore conclude that web users should vigilantly look for the best search engine on which their information needs will be fully met with less or little response time and distractions. Results obtained in this study cannot be generalized for now, since it is centered around the keywords or queries from Computer Science profession. Further works in some other professions are still needed to be done in order to clarify and establish the claims reported in this study.

Acknowledgements

Students of the Department of Computer Science, University of Ibadan, Nigeria, are acknowledged for carrying out this study diligently with the researcher. The study was done in partial fulfillment of the course CSC392 (Computer Applications, 2008/09 Session), during which the author supervised, collated and analyzed the findings of the study.

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THE GALOIS GROUP OF THE CHEBYSHEV POLYNOMIALS OF THE FIRST KIND OF PRIME DEGREE

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ABSTRACT

The Galois Group of a polynomial $p(x)$ is a group associated with $p(x)$. It is a discrete structure arising from the algebraic Galois Theory of Equations. The Galois Group provides a connection between the algebraic theories of fields and groups. There is a close relationship between the roots of a polynomial and its Galois Group, to wit, the Galois Group of a polynomial refers to a certain permutation group of the roots of the polynomial. In this paper, it is shown that the Galois group of the Chebyshev polynomials of the first kind of prime degree over the field of rationals (a field of zero characteristic) is isomorphic to the cyclic group of order two. The result is established via the concept of a splitting field.

Keywords and Phrases: Galois group, Splitting field, Chebyshev polynomials of the first kind, Cyclic group.
I. INTRODUCTION

The Galois Group of a polynomial p(x) is a group associated with p(x). It is a discrete structure arising from the Galois Theory of Equations, which is due to the French scientist, Evariste Galois (1811 – 1832). The Galois Group provides a connection between the algebraic theories of fields and groups. There is a close relationship between the roots of a polynomial and its Galois Group, to wit, the Galois Group of a polynomial refers to a certain permutation group of the roots of the polynomial [8]. Algorithms [e.g. see 6, 7] and application software (e.g. MAPLE) exist for computing the Galois Group of a polynomial.

In a much earlier work, Schur [16] derived relations for the Galois Group of the exponential Taylor polynomials and showed that:

$$G (K, F) = \begin{cases} A_n & \text{if } n \equiv 0 \pmod{4} \\
S_n & \text{otherwise} \end{cases}$$

where $S_n$ is the symmetric group on n letters and $A_n$ the alternating group of degree n. This result was re-established by Coleman [5] using the concept of p-adic Newton polygons. The Galois Groups of the generalized Puiseux expansions and of periodic points are respectively discussed in [12] and [19] whilst some results on the p – adic theory of exponential sums are presented in [17].

The Galois Group structure of the Chebyshev polynomials of the first kind over a field of characteristic p (where p is a prime) has been directly or indirectly investigated by various authors including Cohen [4], Matthew [10], Niederreiter [13] and Abhyankar [1]. In [2], it was shown that various finite classical groups can be realized as Galois Groups of specific concrete polynomials using the theorems of Cameron and Kantor. To the best of the author’s knowledge, there is hitherto no published result on the Galois Group of the Chebyshev polynomials (of the first kind) over a field of zero characteristic.

In this paper therefore, the splitting field of the Chebyshev polynomials of the first kind of prime degrees over a field of zero characteristic (the rationals Q) is first deduced, and then it is shown that the Galois Group of these polynomials over Q is isomorphic to the cyclic group of order two. Joint properties of the Chebyshev polynomials of the first and second kinds can be found in [18].

II. PROPERTIES OF THE CHEBYSHEV POLYNOMIALS OF THE FIRST KIND

The Chebyshev polynomials of the first kind of degree r, $T_r(x)$, are generally defined by [11].

$$T_r(x) = \left( x + \sqrt{x^2 - 1} \right)^r + \left( x - \sqrt{x^2 - 1} \right)^r$$

(2.1)

The polynomials also satisfy the recurrence equation [8]:

$$T_{r+1}(x) = 2x T_r(x) - T_{r-1}(x)$$

(2.2)

and are defined in the interval [1,1]
The zeros of the polynomials are given by [9].

\[ x_j^{(r)} = \cos \left( \frac{2j - 1)\pi}{2r} \right) \quad (2.3) \]

where \( j = 1, 2, \ldots, n \).

Other algebraic and number theoretic properties of \( T_r(x) \) include the following [3, 14]:

(i) \( T_r(x) \) is irreducible over \( \mathbb{Q} \) (the rationals) only if \( r = 2^k \) where \( k = 0, 1, 2, \ldots \)

(ii) \( T_{2j + 1}(x) \) is reducible over \( \mathbb{Q} \) where \( j = 1, 2, \ldots \).

(iii) \( T_r(T_s) = T_s(T_r) \)

(iv) \( T_r(T_s(x)) = T_{rs}(x) \)

(v) If \( r \geq 2 \), then only the Chebyshev polynomials of the first kind can commute with a given \( T_r(x) \)

(vi) The leading term in \( T_r(x) \) is always \( 2^{r-1} x^r \)

(vii) \( |T_r(x)| \leq 1 \)

(viii) \( T_r(x_v) = (-1)^v \)

(ix) If \( x \in \mathbb{N} \) (set of natural numbers) and \( p \) is an odd prime, then \( T_p(x) \equiv T_1(x) \pmod{p} \)

It can be noted that (iii) and (iv) are respectively the commutative and semigroup property of \( T_r(x) \) whilst (ix) is the Fermat’s Theorem for the Chebyshev polynomials.

III. GALOIS GROUP

In this section, the main results on the Galois Group of the Chebyshev polynomials of the first kind over a field of zero characteristic, \( \mathbb{Q} \), is presented. The results revolve round the concept of a splitting field [8, 15].

**Definition 3.1**

Let \( F[x] \) be the field of polynomials in the indeterminate \( x \) and \( f(x) \in F[x] \). Then a finite extension \( K \) of \( F \) is said to be a splitting field over \( F \) for \( f(x) \) if \( f(x) \) can be expressed as a product of linear factors over \( K \) but not over any intermediate field between \( F \) and \( K \).

**Remark 3.2**

Given any polynomial \( f(x) \) over a fundamental field \( F[x] \), a splitting field \( K \) for \( f(x) \) over \( F \) (in which \( f(x) \) has \( n \) zeros) is always guaranteed such that \( [K:F] \leq n! \) where \( [K:F] \) is the dimension of the vector space \( K \) over \( F \).

**Definition 3.3**

A field \( F \) is said to be of characteristic zero if \( nx \neq 0 \) \( \forall x \neq 0, n > 0 \), where \( x \in F \) and \( n \in \mathbb{Z} \) (the set of integers). If \( \exists n > 0 \) such that \( nx = 0 \) \( \forall x \in F \), then \( F \) is said to be of finite characteristic.

**Theorem 3.4**

Let \( p, q \) be primes. Then

\[ \sqrt{x_1 + y \sqrt{(p'q')}} \equiv x_2 \sqrt{q'} + y_2 \sqrt{p} \]
where \( x_1, y_1, x_2, y_2 \in \mathbb{R} \) (the set of real numbers) and \( r, s, t \in \mathbb{N} \) (the set of natural numbers)

**Proof**

By squaring the LHS of the equation:

\[
x_1^2 + y_1^2 p^r q^s + 2x_1 y_1 \sqrt{(p^r q^s)}
\]

Similarly, the RHS becomes

\[
x_2^4 q^t + y_2^4 p + 2x_2^2 y_2^2 q^t
\]

By putting \( x_1 = y_2 \sqrt{p} \), \( y_1 = x_2^2 \), \( p^r = q^t \) and \( s = t \), the result follows. □

**Theorem 3.5**

Let \( T_r(x) \) be the Chebyshev polynomials of the first kind of prime degree \( p \). Then the splitting field \( K \) of \( T_r(x) \) over \( \mathbb{Q} \) (the rationals) is

\[
K = \mathbb{Q}(\sqrt{p})
\]

**Proof**

This follows from the fact that the zeros of the polynomials are given by:

\[
x_j(r) = \cos((2j-1)/2r)
\]

where \( j = 1, 2, \ldots, n \). □

**Definition 3.6**

The Galois Group \( G(K,F) \) of a polynomial \( f(x) \in F[x] \) in which \( K \) is the splitting field over \( F \) is the group of all the automorphisms of \( K \) which leaves every element of \( F \) fixed.

**Theorem 3.7**

Let \( F = \mathbb{Q} \) be the fundamental field and \( K \) the splitting field of \( T_r(x) \), the Chebyshev polynomials of the first kind of prime degree. Then the Galois Group \( G(K,F) \) of \( T_r(x) \) is isomorphic to the cyclic group of order 2.

**Proof**

By Theorem 3.4, \( K = \mathbb{Q}(\sqrt{p}) \). Let \( \sigma \) be an automorphism of \( K \). Now,

\[
\mathbb{Q}(\sqrt{p}) = \{ a + b \sqrt{p} : a, b \in \mathbb{R} \}
\]

And so \( \sigma(\sqrt{p}) = \pm \sqrt{p} \) where \( \mathbb{R} \) is the set of real numbers.

Suppose \( \sigma(a) = a \) and \( \sigma(b) = b \) \( \forall a, b \in \mathbb{R} \)

Then

\[
\sigma(a + b \sqrt{p}) = \sigma(a) + \sigma(b \sqrt{p})
\]

\[
= \sigma(a) + \sigma(b) \sigma(\sqrt{p})
\]

\[
= a \pm b \sqrt{p}
\]

i.e. \( \sigma_1 = (a \pm b \sqrt{p}) = a + b \sqrt{p} \) and \( \sigma_2 = (a + b \sqrt{p}) = a - b \sqrt{p} \)

where \( \sigma_1 \) is the identity automorphism.

\[
\therefore G(K,F) = \{ \sigma_1, \sigma_2 \} \text{ and so } |G(K,F)| = 2
\]

Hence the result, since \( \exists \) only 1 group of order 2 up to isomorphism. □
IV. CONCLUSION

It has been shown in this paper that the Galois Group of the Chebyshev polynomials of the first kind over the field of rationals \( \mathbb{Q} \) is isomorphic to the cyclic group of order 2 when the degree of the polynomials is prime. This result was deduced directly from a consideration of the splitting field of the polynomials over \( \mathbb{Q} \).

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PATCHED SEGMENTED COLLOCATION TECHNIQUES FOR THE NUMERICAL SOLUTION OF SECOND ORDER BOUNDARY VALUE PROBLEMS

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ABSTRACT

This paper deals with the numerical solutions of boundary value problems by patched segmented collocation method. The method examined the numerical solutions of boundary value problems after the whole intervals of consideration have been partitioned into various sub-intervals and the solutions are sought in the various sub-intervals and then matched together using Chebyshev polynomials as the basis function. Numerical examples are given to illustrate the efficiency, accuracy and computational cost of the method. Results obtained are better than when the problems are solved within the whole intervals using the same approach.

Keywords: Patched Segmented Collocation Method, Boundary value problems, Chebyshev Polynomials, Accuracy and Approximation.
I. INTRODUCTION

The primary aim of this paper is to provide efficient and reliable methods for obtaining numerical solutions to problems that prove difficult in getting their solutions in closed form. For the purpose of our discussion, we have investigated the numerical solutions of second order boundary value problems of the form:

\[ P(x)y''(x) + Q(x)y'(x) + R(x)y(x) = f(x), \quad a \leq x \leq b \]  

(1)

together with the conditions

\[ y(a) = A \]  

(2)

and

\[ y(b) = B \]  

(3)

where \( y(a) \), \( y(b) \), \( A \) and \( B \) are known values which are valid in some intervals \( a \leq x \leq b \) together with sufficient conditions imposed on the dependent variable at the two ends points \( x=a \) and \( x=b \), where \( x \) is the independent variable , \( y(x) \) is an unknown function, \( P(x) \), \( Q(x) \), \( R(x) \) and \( f(x) \) are known smooth functions. Active research works have extensively being carried out in this area. Among the well known methods are Weighted Residual Galerkin, Collocation, Finite Element with power series and Canonical forms as basis functions, to mention a few (see\[ 2,3,5,6\]).

In this paper, we have investigated the same class of problems by partitioning the given intervals into segments and the sought results in these segments using Chebyshev Polynomials of degree \( N \) as our basis. We then patched the solutions together to give our required approximate solution. Here, we have used two numerical methods namely Standard and Perturbed methods without segmentation and Standard and Perturbed Patched Segmented collocation methods.

II. STANDARD COLLOCATION METHOD WITHOUT SEGMENTATION (SCMWS)

This method was discussed in [2]. In order to apply this method, we assume an approximate solution of the form:

\[ y_N(x, a) = \sum_{i=0}^{N} a_i T_i(x) \]  

(4)

where \( x \) represents the independent variables in the problem and the functions

\[ T_0(x), T_1(x), \ldots, T_N(x) \]

are Chebyshev Polynomials defined in the interval \([a,b]\) by

\[ T_r(x) = \cos\left( r \cos^{-1}\left( \frac{2(x-a)}{b-a} \right) - 1 \right) \]  

(5)

In order to solve equations (1)-(3), we substitute equations (2) and (3) into equation (4), we obtain,

\[ y_N(x, a) = \sum_{i=0}^{N} a_i T_i(x_a) = A \]  

(6)

and,
\[ y_n(x,b) \approx \sum_{i=0}^{N} a_i T_i(x_b) = B \]  
(7)

Making \( a_0 \) the subject in equation (6), we obtain

\[ a_0 = \frac{1}{T_0(x)} \left[ A - \sum_{i=1}^{N} a_i T_i(x_a) \right] \]  
(8)

Thus, substituting equation (8) into equation (7), after simplification, we obtain,

\[ a_i = \frac{1}{T_0(x_b) T_i(x_a) - T_0(x_a) T_i(x_b)} \left\{ (T_0(x_b) A - T_0(x_a) B) - \sum_{i=2}^{N} a_i (T_i(x_a) T_{i-2}(x_b) - T_{i-2}(x_a) T_i(x_b)) \right\} \]  
(9)

Hence, substituting equation (9) into equation (8), after simplification, we obtain,

\[ a_0 = \frac{1}{T_0(x_a)} \left\{ A - \frac{T_i(x_a)}{T_0(x_b) T_i(x_a) - T_0(x_a) T_i(x_b)} \left( (T_0(x_b) A - T_0(x_a) B) \right) \right\} - \sum_{i=2}^{N} a_i (T_i(x_a) T_{i-2}(x_b) - T_{i-2}(x_a) T_i(x_b)) \]  
(10)

Finally, substituting equations (9) and (10) into equation (4) after simplification, we obtain,

\[ a_0 = \frac{1}{T_0(x_a)} \left\{ A - \frac{T_i(x_a)}{T_0(x_b) T_i(x_a) - T_0(x_a) T_i(x_b)} \left( (T_0(x_b) A - T_0(x_a) B) \right) \right\} - \sum_{i=2}^{N} a_i (T_i(x_a) T_{i-2}(x_b) - T_{i-2}(x_a) T_i(x_b)) \]  
(10)

Finally, substituting equation (9) into equation (8), after simplification, we obtain,

\[ y_n(x,a) = \frac{T_0(x)}{T_0(x_a)} \left\{ A - \frac{T_i(x_a)}{T_0(x_b) T_i(x_a) - T_0(x_a) T_i(x_b)} \left( (T_0(x_b) A - T_0(x_a) B) \right) \right\} - \sum_{i=2}^{N} a_i (T_i(x_a) T_{i-2}(x_b) - T_{i-2}(x_a) T_i(x_b)) \]  
(11)
We thus substitute equation (11) into equation (1), we obtain

\[ P(x)y''(x,a) + Q(x)y'(x,a) + R(x)y(x,a) = f(x) \]

(12)

Equation (12) is then collocated at points \( x = x_k \), we obtain

\[ P(x_k)y''(x_k,a) + Q(x_k)y'(x_k,a) + R(x_k)y(x_k,a) = f(x_k) \]

(13)

where,

\[ x_k = a + \frac{(b-a)k}{N}, \quad j = 1, 2, 3, \ldots, N - 1 \]

(14)

and \( a, b \) are respectively the lower and upper bounds of the interval. Hence, equation (13) gives rise to \((N-1)\) linear systems of algebraic equations in \((N-1)\) unknown constants \( a_i \) \((i = 2, 3, \ldots, N)\) which are then solved by Gaussian Elimination method to obtain the values of \( a_i \) \((i = 2, 3, \ldots, N)\). The obtained values are then substituted back into our approximate solution given by equation (11).

**III. PERTURBED COLLOCATION METHOD WITHOUT SEGMENTATION (PCMWS)**

The whole idea of the perturbed collocation method is the addition of a small perturbed term, \( H_N(x) \) as conceived by Lanczos [1] to equation (12). Thus, equation (12) now becomes

\[ P(x)y''_N(x,a) + Q(x)y'_{N(x,a)} + R(x)y_N(x,a) = f(x) + H_N(x) \]

(15)

where,

\[ H_N(x) = \tau_1 T_{N+2}(x) + \tau_2 T_{N+1}(x) \]

Here \( \tau_1 \) and \( \tau_2 \) are tau-parameters to be determined and \( T_N(x) \) are Chebyshev polynomials defined by equation (5). Thus equation (15) is then collocation at points \( x_j \), we obtain

\[ P(x_j)y''_N(x_j,a) + Q(x_j)y'_{N(x_j,a)} + R(x_j)y_N(x_j,a) = f(x_j) + \tau_1 T_{N+2}(x_j) + \tau_2 T_{N+1}(x_j) \]

(16)

where,

\[ x_j = a + ((b-a)j)/(N+2), \quad j = 1, 2, 3, \ldots, N+1 \]

Hence, equation (16) gives rises to \((N + 1)\) linear systems of algebraic equations in \((N+1)\) unknown constants \( a_i \) \((i = 2, 3, \ldots, N)\) \( \tau_1 \) and \( \tau_2 \). Also, these linear systems of algebraic equations are then solved using Gaussian elimination method to obtain the \( N + 1 \) unknown constants which are then substituted back into our approximate solution.
In this section, we consider the general second order differential equation of the form given in equation (1) together with the boundary conditions given in equations (2) and (3). Also, our approximate solution given by equation (4) is modified as follows:

\[ y_{mN}(x) = y_{1N}(x) U \ y_{2N}(x) U \ldots \ldots U \ y_{mN}(x) \]

where,

\[ y_{1N}(x) = \sum_{i=0}^{N} a_i T_{1N}(x), \quad x_a \leq x \leq x_i \]

(18)

\[ y_{2N}(x) = \sum_{i=0}^{N} a_i T_{2N}(x), \quad x_i \leq x \leq x_2 \]

(19)

\[ y_{mN}(x) = \sum_{i=0}^{N} a_i T_{mN}(x), \quad x_m \leq x \leq x_N = x_b \]

(20)

and \( m \) denotes the number of segments. To solve equation (1) in the first segment, a new condition is now added at the inter segment points to the initial condition given by equation (1), that is,

\[ y(x_i) = A_1 \]

(21)

where \( A_1 \) is the solution at \( x = x_1 \) in case the exact solution is known otherwise we forced the derivative to be equal to the initial condition. That is,

\[ y(x_i) = y'(x_1) \]

Thus, putting equations (2) and (21) into equation (18), after simplification, we obtain,

\[ y_{1N}(x_a, a) \approx \sum_{i=0}^{N} a_i T_{1i}(x_a) = A \]

(22)

and

\[ y_{1N}(x_i, a) \approx \sum_{i=0}^{N} a_i T_{1i}(x_i) = A_i \]

(23)

Making \( a_{i0} \) the subject of the formula in equation (22), we obtain,

\[ a_{i0} = \frac{1}{T_{i0}(x)} \left[ A - \sum_{i=0}^{N} a_i T_{1i}(x_a) \right] \]

(24)
Thus, substituting equation (24) into equation (23), after simplification and make \( a_{ii} \) the subject, we obtain,

\[
a_{11} = \frac{1}{T_{10}(x_1)T_{11}(x_a) - T_{10}(x_a)T_{11}(x_1)} \left\{ \frac{T_{11}(x_a)}{T_{10}(x_1)} - \frac{T_{11}(x_a)}{T_{10}(x_a)} \right\} \left( (T_{10}(x_1)A - T_{10}(x_a)A_i) - \sum_{i=2}^{N} a_{ii}(T_{ii}(x_a)T_{i-2}(x_1) - T_{ii}(x_a)T_{i-2}(x_1)) - \sum_{i=2}^{N} a_{ii}T_{ii}(x_a) \right) \right\} \tag{25}
\]

Hence, putting equation (25) into equation (24), after simplification, we obtain,

\[
a_{10} = \frac{1}{T_{10}(x_a)} \left\{ \frac{T_{11}(x_a)}{T_{10}(x_1)T_{11}(x_a) - T_{10}(x_a)T_{11}(x_1)} \right\} \left( (T_{10}(x_1)A - T_{10}(x_a)A_i) - \sum_{i=2}^{N} a_{ii}(T_{ii}(x_a)T_{i-2}(x_1) - T_{ii}(x_a)T_{i-2}(x_1)) - \sum_{i=2}^{N} a_{ii}T_{ii}(x_a) \right) \right\} \tag{26}
\]

Finally, substituting equations (25) and (26) into equation (18), thus reducing the number of unknown constants \( a_{ii} (i = 2, 3, ..., N) \) to \( a_{ij} (j = 2, 3, ..., N - 1) \). That is,

\[
y_{N} (x, a) = \frac{T_{10}(x_a)}{T_{10}(x_a)} \left\{ \frac{T_{11}(x_a)}{T_{10}(x_1)T_{11}(x_a) - T_{10}(x_a)T_{11}(x_1)} \right\} \left( (T_{10}(x_1)A - T_{10}(x_a)A_i) - \sum_{i=2}^{N} a_{ii}(T_{ii}(x_a)T_{i-2}(x_1) - T_{ii}(x_a)T_{i-2}(x_1)) - \sum_{i=2}^{N} a_{ii}T_{ii}(x_a) \right) \right\} \tag{27}
\]

Thus equation (27) is our new approximate solution in the first segment with \( N - 1 \) unknown constants. Thus equation (27) is then substituted into equation (1) to obtain,

\[
P(x)y_{1N}^+(x, a) + Q(x)y_{1N}^+(x, a) + R(x)y_{1N}^+(x, a) = f(x) \tag{28}
\]

We then collocate equation (28) at the point \( x = x_j \), we obtain,

\[
P(x_j)y_{1N}^+(x_j, a) + Q(x_j)y_{1N}^+(x_j, a) + R(x_j)y_{1N}^+(x_j, a) = f(x_j) \tag{29}
\]
where

\[ x_j = a + \frac{(x_i - a)j}{N}, \quad j = 1, 2, 3, ..., N - 1 \]  

(30)

Thus, the collocation equation (29) gives rise to N-1 linear algebraic systems of equations in N-1 unknown constants. These equations are then solved by Gaussian Elimination to obtain the values of unknown constants which are then substituted back into equation (27) to obtain our approximate solution at the first segment. The process is repeated until the solutions are obtained throughout the other segments.

V. PATCHED PERTURBED SEGMENT COLLOCATION METHOD (PPSCM)

In this section, a perturbation parameter \( H_{1N}(x) \) is added to equation (28), we obtain,

\[ P(x)y_{1N}^+(x,a) + Q(x)y_{1N}^-(x,a) + R(x)y_{1N}^0(x,a) = f(x) + H_{1N}(x) \]  

(31)

where,

\[ H_{1N}(x) = \tau_{10}T_{1N+2}(x) + \tau_{11}T_{1N+1}(x) \]

and \( \tau_{10} \) and \( \tau_{11} \) are free tau parameter to be determined. We then collocate equation (31) at the point \( x=x_k \), we obtain,

\[ P(x_k)y_{1N}^+(x_k,a) + Q(x_k)y_{1N}^-(x_k,a) + R(x_k)y_{1N}^0(x_k,a) = f(x_k) + \tau_{10}T_{1N+2}(x_j) + \tau_{11}T_{1N+1}(x_k) \]  

(33)

where,

\[ x_k = a + \frac{(x_i - a)k}{N + 1}, \quad k = 1, 2, 3, ..., N + 1 \]

Hence, the collocated equation (33) gives rise to N+1 linear algebraic systems of equations in N+1 unknown constants. These N+1 linear algebraic equations are then solved using Gaussian Elimination to obtain the values of the N+1 unknown constants which are then substituted back into our new approximate solution of equation (27).
VI. NUMERICAL EXAMPLES

Example 1: Solve the following problem:

\[ 12x^2 \ y''(x) + 24 \ y'(x) = -3x^4 + 204x^3 - 351x^2 + 11x, \quad 0 \leq x \leq 1 \]

with the boundary conditions,

\[ y(0) = 1 \ and \ y(1) = 2 \]

\[ y(x) = \frac{1}{24} (-3x^4 + 34x^3 - 117x^2 + 110x + 24) \]

Fig. 1 Graphical representation of the exact solution and the other approximate solutions.
Example 2:

\[ x^3 y'''(x) + x^2 y'(x) - 2 = 0, \quad 1 \leq x \leq 2 \]

\[ y(1) = 2 \]

\[ -x y'(x) \big|_{x=2} = \frac{1}{2} \]

\[ y(x) = \frac{2}{x} \ln(x) + \frac{1}{2} \]

Fig. 2 Graphical representation of example 2 for the exact solution and other approximate solutions.
VII. CONCLUSION

In this paper, patched segmented collocation methods have been successfully applied to solve linear Boundary Value Problems. It was shown that these methods were very efficient and powerful to get closer to the solution as this can be seen from the graphs. We observed that as N increases, the numerical solution of the two methods tends towards the exact solution but the patched perturbed segmented collocation method moved closer to the exact solution than other method. Also, the two graphs show the accuracy of the methods as compared with the exact solution.

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A NOTE ON THE ALGEBRA OF QUALITATIVE EQUIVALENCE OF ORDINARY DIFFERENTIAL EQUATIONS

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ABSTRACT

The notion of qualitative equivalence of ordinary differential equations is a concept which assists in describing the behavior of an equation without necessarily drawing the solution curves of the equation. This is achieved via the geometrical representation of the equation. Qualitative equivalence of a set of differential equations necessarily results into the generation of the qualitative classes of the set – a discrete structure. Practical areas of application of this concept include computer networking, fractals and coding theory. In this paper, the basic principle of the idea is presented using a simple illustration, namely, the qualitative equivalence behavior of the equation \( x' = x(1-a) + b \), where \( a, b \in \mathbb{IR} \), from the point of view of the equilibrium point of the equation. It is shown that the phase portrait of the set \( S = \{ x' = x(1-a) + b : a, b \in \mathbb{IR} \} \) of first order autonomous ordinary differential equations is an attractor if \( a > 0 \) and a repellor if \( a \leq 0 \). It is also shown that \( S \) has two qualitative classes. Furthermore, qualitative equivalence is established between some subsets of \( S \) and some subsets of the universal set \( L = \{ x' = ax + b : a, b \in \mathbb{IR} \} \) of first order linear autonomous ordinary differential equations.

Keywords and phrases: Qualitative equivalence, first order autonomous ordinary differential equations, qualitative classes, phase portrait, equilibrium point.
I. INTRODUCTION

The notion of qualitative equivalence of ordinary differential equations is a concept which assists in describing the behavior of an equation without necessarily drawing the solution curves of the equation. This is achieved via the geometrical representation of the equation. Qualitative equivalence of a set of differential equations necessarily results into the generation of the qualitative classes of the set – a discrete structure. Practical areas of application of this concept include computer networking and coding theory. In this paper, the author studies the qualitative equivalence characteristics of the solutions of first order autonomous ordinary differential equation \( x' = x(1 - a) + b \), where \( a, b \in \mathbb{I}R \) from the point of view of the equilibrium point of the equation. The paper is based on the existence and uniqueness properties of solutions.

Let \( f : \mathbb{I}R \rightarrow \mathbb{I}R \) be a continuous function. Consider the general first order autonomous equation

\[
x' = f(x)
\]

(1.1)

We seek to describe the behavior of the solutions of (1.1) without necessarily drawing the solution curves of the equation. The approach is to give a geometrical representation of the qualitative behavior of the equation [1]. This representation is called the phase portrait or phase diagram. Of central importance in drawing the phase portrait is the knowledge of the equilibrium point of (1.1). An equilibrium point (or critical point or singular point or stationary point) of (1) is the point \( c \) such that \( f(c) = 0 \). The phase portrait of any equation of the form (1.1) is completely determined by the nature of its equilibrium points. By the Fundamental Theorem of Algebra and its Corollary [2], the maximum number of equilibrium points of (1.1) is the same as the degree of \( f(x) \). In general, the phase portrait of an equilibrium point \( c \) of (1.1) can only be one of the following viz attractor, repellor, positive shunt and negative shunt. These are called the qualitative types [4, 6].

II. MAIN RESULTS

This section contains the main results of the paper

Definition 2.1 [4]

Let

\[
x' = f(x)
\]

(2.1A)

and

\[
y' = g(y)
\]

(2.1B)

be two first order autonomous ordinary differential equations. Then the two equations are said to be qualitatively (or topologically) equivalent if there exists a continuous bijection from the phase portrait of (2.1A) onto the phase portrait of (2.1B) in such a way that the orientation of the phase portraits is preserved.
Theorem 2.2 [4]

Let $E_1$ and $E_2$ be two first order autonomous ordinary differential equations. Then the two equations are qualitatively equivalent if they have the same qualitative type.

Proof

Suppose $E_1$ and $E_2$ have the same phase portrait. Then an orientation preserving continuous bijections can be defined from the phase portrait of $E_1$ onto that of $E_2$. Therefore $E_1$ and $E_2$ are qualitatively equivalent. □

Theorem 2.3 [4]

Suppose $E_1$ and $E_2$ are two first order autonomous ordinary differential equations. Let $E_1 \sim E_2$ iff $E_1$ is qualitatively equivalent to $E_2$. Then $\sim$ defines an equivalence relation.

Proof

This follows from the fact that $\sim$ is reflexive, symmetric and transitive □

We now consider the set

$L = \{ x' = f(x) \mid f: \text{IR} \rightarrow \text{IR} \}$

of first order autonomous ordinary differential equations, where IR is the set of real numbers. By the Fundamental Theorem of Equivalence Relations [2, 3], $L$ is partitioned into disjoint equivalence classes called qualitative classes. All equations which belong to the same qualitative class exhibit the same qualitative behavior. This behavior gives a description of the existence and uniqueness properties of the solutions of (1.1). The qualitative behavior is essentially determined by the function $f$.

Theorem 2.4

Let

$S = \{ x' = f(x) = x(1 - a) + b : a, b \in \text{IR} \}$

be a set of first order autonomous ordinary differential equations. Then

(i) The phase portrait of $S$ is an attractor if $a > 0$ and it is a repellor if $a \leq 0$.

(ii) $S$ has two qualitative classes.

Proof

(i) We define the following subsets of $S$ :

$S_1 = \{ x' = x(1 - a) + b : a > 0, b > 0 \}$

$S_2 = \{ x' = x(1 - a) + b : a < 0, b > 0 \}$

$S_3 = \{ x' = x(1 - a) + b : a > 0, b < 0 \}$

$S_4 = \{ x' = x(1 - a) + b : a < 0, b < 0 \}$

$S_5 = \{ x' = x(1 - a) + b : a = 0, b > 0 \}$

$S_6 = \{ x' = x(1 - a) + b : a = 0, b < 0 \}$

$S_7 = \{ x' = x(1 - a) + b : a > 0, b = 0 \}$
S_8 = \{x' = x(1 - a) + b : a < 0, b = 0\}

S_9 = \{x' = x(1-a) + b : a = b = 0\}

where S = US_i and S_i \cap S_j = \emptyset for all 1 \leq i \leq 9, 1 \leq j \leq 9, i \neq j. We note that the equilibrium point of S is \(-b/(1-a)\). Consider S_1, S_3 and S_7 which are subsets of S in which a > 0. When x > -b/(1-a) (or < -b/(1-a)), f(x) < 0 (or > 0) respectively, where a \neq 1. The phase portrait of each of S_1, S_3 and S_7 is thus an attractor. Suppose a \leq 0 and consider S_2, S_4, S_5, S_6, S_8 and S_9. When x > -b(1-a) (or < -b(1-a)), f(x) > 0 (or < 0) respectively. Therefore, the phase portrait of each of these subsets is a repellor. Hence the result. □

(ii) That S has two qualitative classes follows from the fact that every subset of S is either an attractor or a repellor. □

**Theorem 2.5**

Let

S* = \{x' = x (1-a) + b : a > 0, a, b \in \mathbb{IR}\}

L* = \{x' = ax + b : a < 0, a, b \in \mathbb{IR}\}

P* = \{x' = x(1-a) + b : a \leq 0, a, b \in \mathbb{IR}\}

Q* = \{x' = ax + b : a > 0, a, b \in \mathbb{IR}\}

be sets of first order linear autonomous ordinary differential equations, where \mathbb{IR} is the set of real numbers. Then S* is qualitatively equivalent to L* and P* is qualitatively equivalent to Q*.

**Proof**

It shall be shown that S* and L* have the same qualitative type and P* and Q* have the same qualitative type. By Theorem 2.4, the phase portrait of S* is an attractor. For L*, f(x) < 0 (or > 0) when x > -b/a (or < -b/a) respectively, and so the phase portrait of L* is an attractor. Also by Theorem 2.4, the phase portrait of P* is a repellor. Now with respect to Q*, f(x) > 0 (or < 0) when x > -b/a (or < -b/a) respectively, and so the phase portrait of Q* is also a repellor. The theorem is thus proved. □

**III. DISCUSSION AND CONCLUSION**

In this paper, the notion of qualitative equivalence has been applied to the set S = \{x' = x(1-a) + b : a, b \in \mathbb{IR}\}, where \mathbb{IR} is the set of real numbers. This set is a subset of the universal set L = \{x' = ax + b : a, b \in \mathbb{IR}\} of first order linear autonomous ordinary differential equations. It is shown that S has two qualitative classes. It is then proved that certain subsets of L are qualitatively equivalent to some subsets of S. The paper gives a description of the qualitative behavior of the equation x' = x(1-a) + b, where a, b \in \mathbb{IR}. Practical application of the notion of qualitative equivalence of a set include computer networking, fractals and coding theory [5, 6, 7].

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